

## CC ALGEBRA <br> CHAPTER 5 - SYSTEM OF EQUATIONS \& INEQUALITIES

- SECTION 5.1 - SYSTEMS OF EQUATIONS IN TWO VARIABLES

Objectives:

- Determine whether an ordered pair is solution of a linear system

- Solve linear systems by substitution
- Solve linear systems by elimination
- Identify systems that do not have exactly one ordered-pair solution
- Solve problems using systems of linear equations

$$
\left\{\begin{aligned}
& x+2 y=2 \\
& x-2 y=6 \\
&(-4,3) \\
&(4,-1)
\end{aligned}\right.
$$

(1) LHS $=4+2(-1)=2=$ RHS
(2) LHS $=4-2(-1)=6=$ RHS $(4,-1)$ is A Soln
(1) LUS $=-4+2(3)=-4+6=2=$ RHS
(2) $\begin{aligned} \text { LHS }= & -4-2(3)=-4-6=-10 \neq R H S=6 x \\ & (-4,3) \text { is NOT A SOLN }\end{aligned}$

## Solving Linear Systems by Substitution

1. Solve either of the equations for one variable in terms of the other. (If one of the equations is already in this form, you can skip this step.)
2. Substitute the expression found in step 1 into the other equation. This will result in an equation in one variable.

3. Solve the equation containing one variable.
4. Back-substitute the value found in step 3 into one of the original equations. Simplify and find the value of the remaining variable.
5. Check the proposed solution in both of the system's given equations.

## Solving Linear Systems by Addition

1. If necessary, rewrite both equations in the form $A x+B y=C$.
2. If necessary, multiply either equation or both equations by appropriate nonzero numbers so that the sum of the $x$-coefficients or the sum of the $y$-coefficients is 0 .

3. Add the equations in step 2 . The sum is an equation in one variable.
4. Solve the equation in one variable.
5. Back-substitute the value obtained in step 4 into either of the given equations and solve for the other variable.
6. Check the solution in both of the original equations.


The Number of Solutions to a System of Two Linear Equations
The number of solutions to a system of two linear equations in two variables is given by one of the following. (See Figure 5.3.)

| Number of Solutions | What This Means Graphically |
| :--- | :--- |
| Exactly one ordered-pair solution | The two lines intersect at one point. |
| No solution | The two lines are parallel. |
| Infinitely many solutions | The two lines are identical. |



Exactly one solution


No solution (parallel lines)


Infinitely many solutions (lines coincide)

FIGURE 5.3 Possible graphs for a system of two linear equations in two variables

